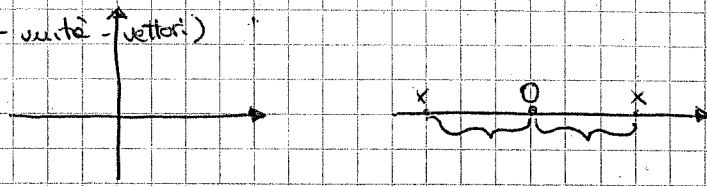


BASI FISICA (grandezze - vettori)
MOTO RETTILINEO.



$$d|x_1 - x_0|$$

Esso deriva $x(t)$

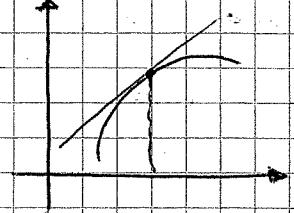
$$v(t) = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \dot{x} = x'$$

derivata = x' , $p'(x)$, x' $\frac{dx}{dt}$

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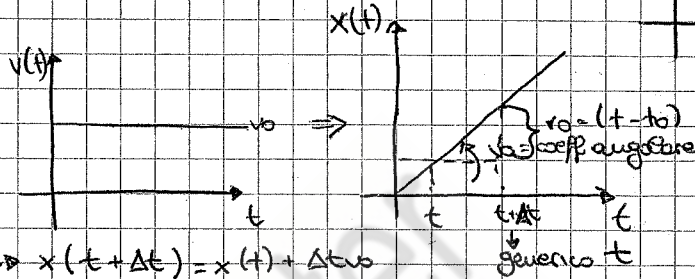
$$v(t) = \lim_{\Delta t \rightarrow 0} \frac{x(t+\Delta t) - x(t)}{\Delta t} \cdot \frac{dx}{dt}$$



MOTO RETTILINEO UNIFORME

$$v = v_0$$

$$v(t) = v_0$$



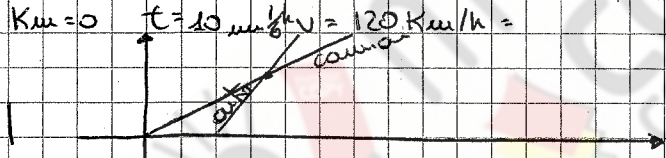
$$v_0 = \frac{x(t + \Delta t) - x(t)}{\Delta t}$$

$$x(t + \Delta t) = x(t) + \Delta t v_0$$

$$x(t) = x(t_0) + (t - t_0) \cdot v_0$$

Camion $K_{m=0}$ $t=0$ $v = 90 \text{ km/h} = 23.3 \text{ m/s}$ dove e quando l'auto supera?

auto $K_{m=0}$ $t = 10 \text{ min}$ $v = 120 \text{ km/h}$



$$\frac{90 \cdot 36}{120 \cdot 23.3} = \frac{120 \cdot 36}{12 \cdot 33.3}$$

$$\frac{120}{108} = \frac{120}{33.3}$$

$$\approx 1.12$$

$$t = 10 \cdot 60 = 600 \text{ s} \rightarrow s = \Delta t \cdot v = 600 \cdot 23.3 = 13900$$

$$\begin{cases} x_t = v_c \cdot t \\ x_A(t) = 0 + v_A(t - t_A) \end{cases} \Rightarrow v_c t = v_A(t - t_A)$$

$$t = \frac{v_A t_A}{v_A - v_c} = \frac{33.3 \cdot 10}{33.3 - 23.3} = \frac{33.3 \cdot 10}{10} = 33.3 \text{ s} = 20 \text{ km} = \frac{2}{3} \text{ h} = 40 \text{ min}$$

$$s_c = \frac{2}{3} \cdot 90 = 60 \text{ km}$$

$$s_a = \left(\frac{2}{3} - \frac{1}{6}\right) \cdot 120 \text{ km} =$$

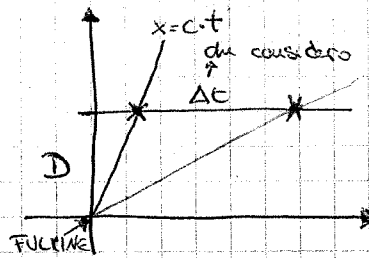
FULMINE $t=0$
TUONO $t=10$ s

$$v = 3 \cdot 10^8 \text{ m/s}$$

$$v_s = 330 \text{ m/s}$$

$$s(s) = v \cdot t = 9 \cdot 330 \text{ m}$$

(La velocità della luce è trascurabile perché molto grande)



$$\begin{cases} D = c t_e \\ D = v_s t_s = v_s (t_e + \Delta t) \end{cases}$$

~~Scegliamo~~ x

$$\frac{D}{c} = v_s (t_e + \Delta t)$$

$$t_e = \frac{v_s}{c} (t_e + \Delta t) = t_e (1 - \frac{v_s}{c}) = \Delta t \cdot \frac{v_s}{c}$$

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$$t_e = \frac{D}{c}$$

$$t_s = \frac{D}{v_s}$$

$$\Delta t = t_s - t_e = \frac{D}{v_s} - \frac{D}{c} = D \left(\frac{1}{v_s} - \frac{1}{c} \right)$$

$$x(t)$$

$$v(t) = \frac{dx}{dt}$$

$$v_{lim} = \frac{\Delta x}{\Delta t} \xrightarrow{\Delta t \rightarrow 0} v(t)$$

$$[v] = L \cdot T^{-1}$$

$$a_{lim} = \frac{\Delta v}{\Delta t} = \frac{v(t + \Delta t) - v(t)}{\Delta t}$$

$$[a] = L \cdot T^{-2}$$

accelerazione: m/s^2 $km/h \cdot s$

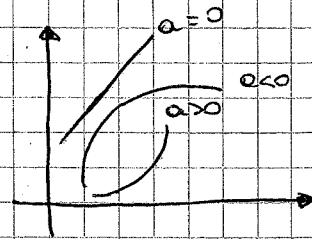
ACCELERAZIONE

$$g = 9.81 \text{ m/s}^2$$

$$a(t) = \lim_{\Delta t \rightarrow 0} \frac{\Delta v}{\Delta t} = \frac{dv}{dt} \text{ retta tangente}$$

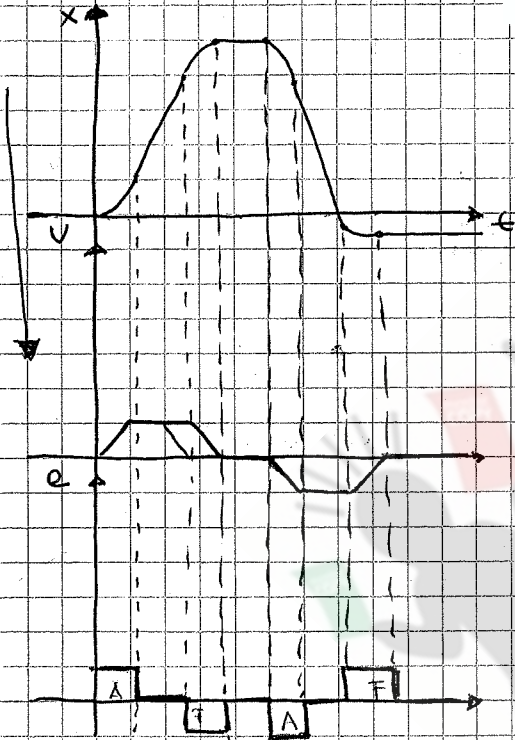
$$\Rightarrow x(t) \frac{d^2x}{dt^2}$$

$$v(t) = \frac{dx}{dt}$$

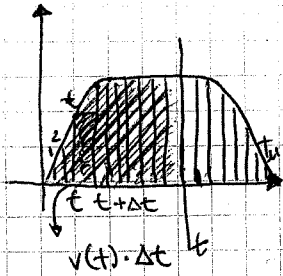


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comosciamo $v(t)$



$$v(t) = \frac{\Delta x}{\Delta t} \quad \Delta x = v(t) \cdot \Delta t$$

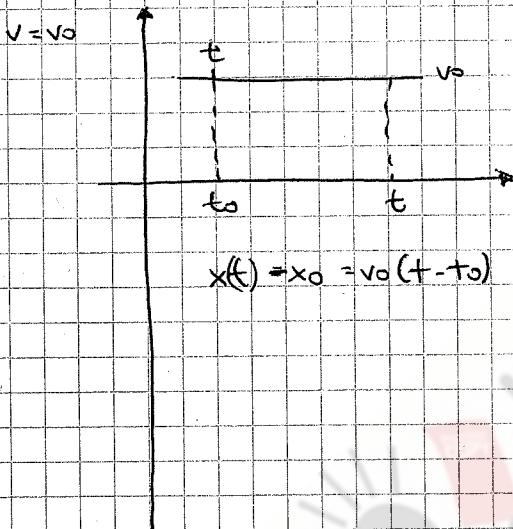
t_0

$$x(t) = x_0 + (x_1 - x_0) + (x_2 - x_1) + \dots + (x_n - x_{n-1})$$

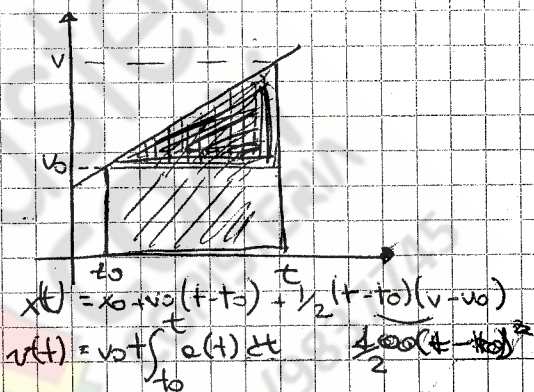
$$x(t) = v(t_0)(t_1 - t_0) + v(t_1)(t_2 - t_1)$$

$$x(t) = x_0 + \sum_{i=1}^{n-1} v(t_i)(t_{i+1} - t_i) = x_0 + \int_{t_0}^t v(t) dt$$

costante
arbitraria
d'integrazione



$$x(t) - x_0 = v_0(t - t_0)$$



$$x(t) = x_0 + v_0(t - t_0) + \frac{1}{2}(t - t_0)(v - v_0)$$

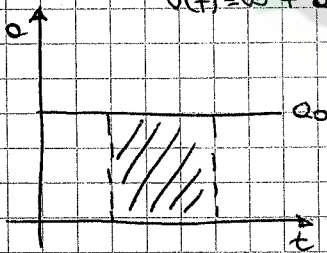
$$v(t) = v_0 + \int_{t_0}^t a(t) dt = \frac{1}{2} a_0 (t - t_0)^2$$

UNIFORMEMENTE ACCELERATO

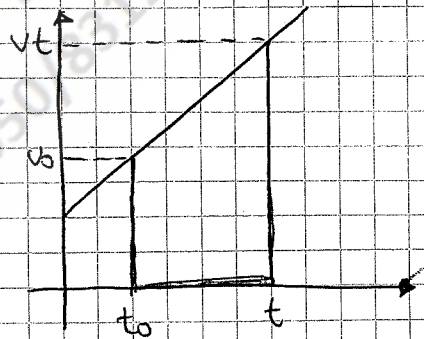
$$a(t) = a_0$$

$$v(t) = v_0 + a_0(t - t_0)$$

$$v(t) = x_0 + v_0(t - t_0) + \frac{1}{2} a_0 (t - t_0)^2$$



$$x(t) = x_0 + v_0(t - t_0) + \frac{1}{2} a_0 (t - t_0)^2$$



$$a_0 = \frac{v - v_0}{t - t_0}$$

$$x(t) - x_0 = \frac{1}{2} (v_0 + v(t)) \cdot (t - t_0)$$

$$x(t) - x_0 = \frac{1}{2} \frac{(v_0 + v(t))}{(t - t_0)} (t - t_0)^2$$

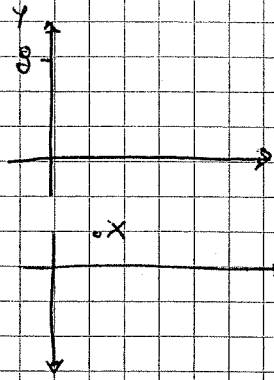
$$(t - t_0) \left[v_0 + \frac{1}{2} v - \frac{1}{2} v_0 \right]$$

$$\frac{1}{2} (t - t_0) [v_0 + v(t)]$$

$$\begin{cases} x(t) = x_0 + v_0(t-t_0) + \frac{1}{2} a_0(t-t_0)^2 \\ v(t) = v_0 + a_0(t-t_0) \end{cases}$$

→ stesso nel campo gravitazionale $\frac{1}{2}g$

FORZE → a



$$y(t) = h + 0 + \frac{1}{2}(-g)t^2$$

$t = y = 0$

$$x(t) = 0 + 0 + \frac{1}{2}gt^2$$

$t = x = \sqrt{\frac{2h}{g}}$

$$x(t) = x_0 + v_0(t-t_0) + \frac{1}{2} a_0 (t-t_0)^2$$

$$v(t) = v_0 + a_0(t-t_0)$$

$$a(t) = a_0$$

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CADUTA DEI GRAVI

$$t = \sqrt{\frac{2h}{g}}$$

$$x_0=0 \quad t_0=0 \quad s$$

v_0 ————— $v(t)$

se conosco t $v(t) = v_0 + a_0(t-t_0)$

se conosco s

$$\begin{cases} s = v_0 t + \frac{1}{2} a_0 t^2 \\ v = v_0 + a_0 t \end{cases}$$

$$v = v_0 + a_0 t$$

$$t = \frac{v - v_0}{a_0}$$

⇓

$$s = v_0 \left(\frac{v - v_0}{a_0} \right) + \frac{1}{2} a_0 \left(\frac{v - v_0}{a_0} \right)^2$$

$$a_0 s = v_0 v - v_0^2 + \frac{1}{2} (v^2 - 2v_0 v + v_0^2)$$

$$a_0 s = \frac{1}{2} v^2 - \frac{1}{2} v_0^2$$

$$v^2 - v_0^2 = 2a_0 s$$

$$v^2 = 2gh$$